

Lessons
3-2 & 3-5

Angles and Parallel Lines



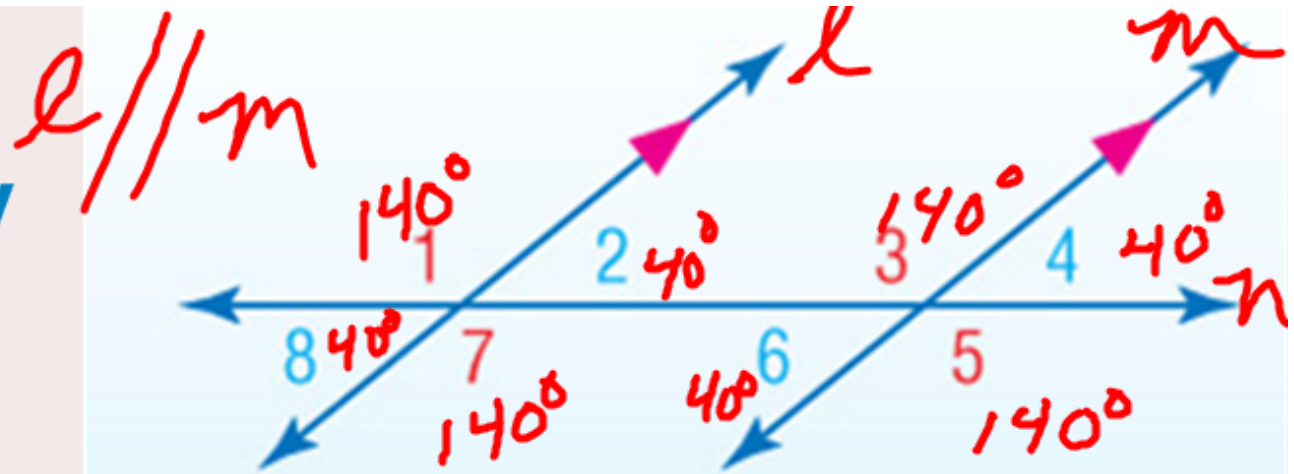
You will use theorems to determine the relationship between special angle pairs.

You will use algebra to find angle measures

You will recognize angle pairs that occur with parallel lines

You will prove that two lines are parallel

If 2 parallel lines are cut by a transversal...



Corresponding angles \cong

$$\angle 1 \cong \angle 3, \angle 5 \cong \angle 7, \angle 8 \cong \angle 6, \angle 2 \cong \angle 4$$

Alt Int angles \cong

$$\angle 2 \cong \angle 6, \angle 7 \cong \angle 3$$

Alt Ext angles \cong

$$\angle 8 \cong \angle 4, \angle 1 \cong \angle 5$$

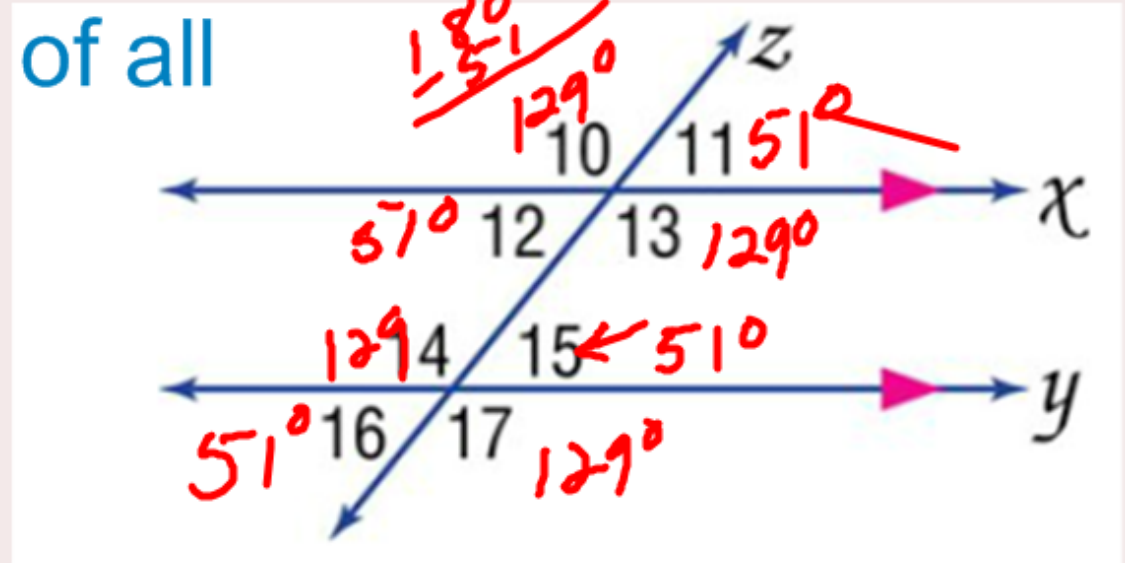
Consec Int

Supplementary

$$m\angle 2 + m\angle 3 = 180$$

$$m\angle 7 + m\angle 6 = 180^\circ$$

In the figure, $m\angle 15 = 51$,
 find the measures of all
 the other \angle 's.



$$m\angle 10 = \underline{129^\circ}$$

$$m\angle 11 = \underline{51^\circ}$$

$$m\angle 12 = \underline{51^\circ}$$

$$m\angle 13 = \underline{129^\circ}$$

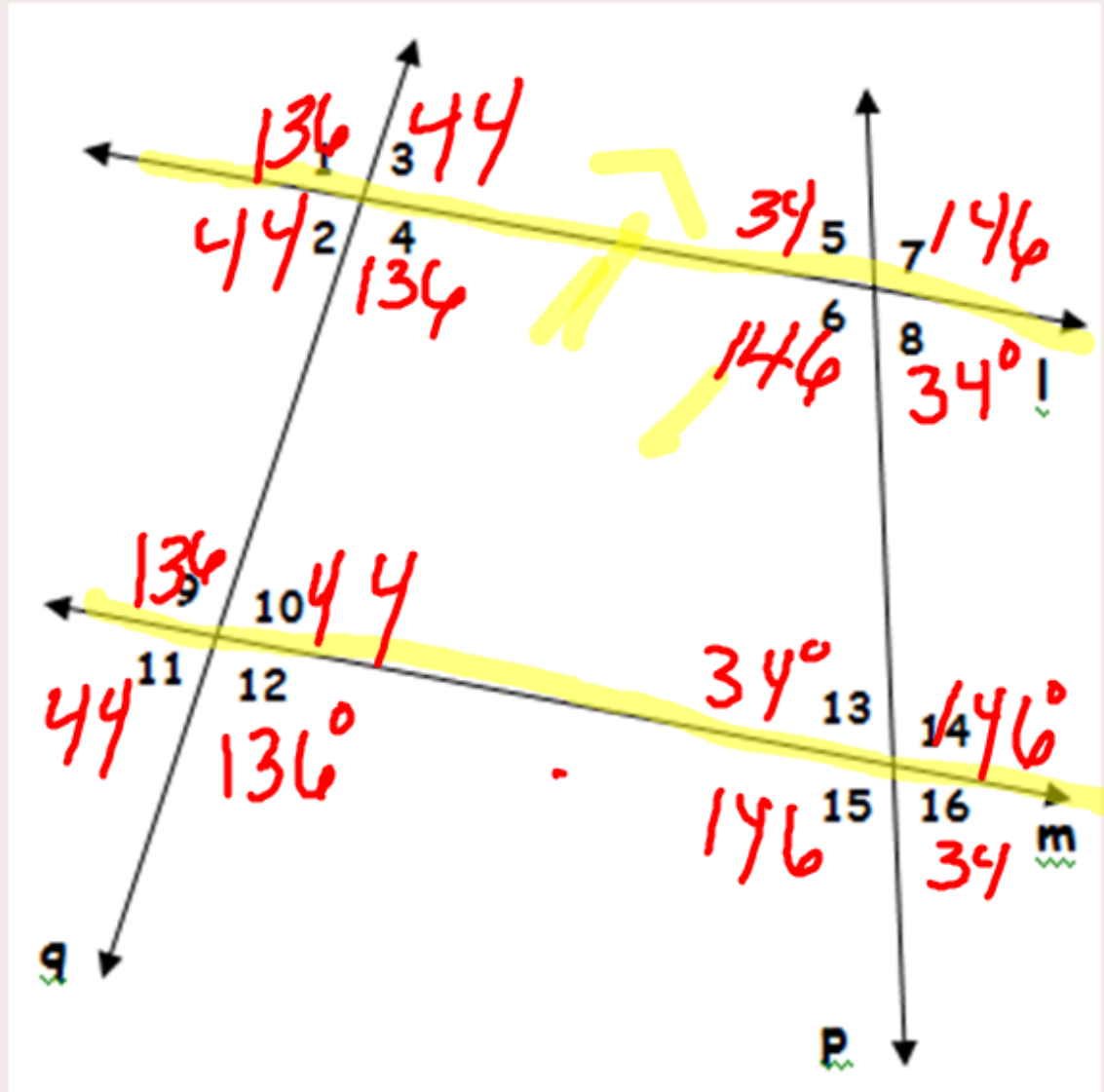
$$m\angle 14 = \underline{129^\circ}$$

$$m\angle 16 = \underline{51^\circ}$$

$$m\angle 17 = \underline{129^\circ}$$

If $l \parallel m$, $m\angle 8 = 34^\circ$ and $m\angle 12 = 136^\circ$, find the measures of the following angles.

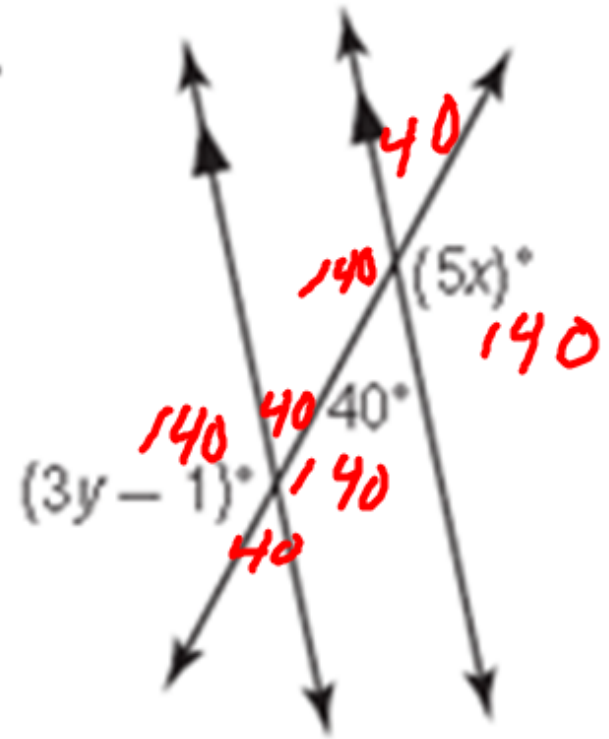
$$\begin{aligned}
 m\angle 1 &= \underline{136^\circ} \\
 m\angle 2 &= \underline{44^\circ} \\
 m\angle 3 &= \underline{44^\circ} \\
 m\angle 4 &= \underline{136^\circ} \\
 m\angle 5 &= \underline{34^\circ} \\
 m\angle 6 &= \underline{146^\circ} \\
 m\angle 7 &= \underline{146^\circ} \\
 m\angle 9 &= \underline{136^\circ} \\
 m\angle 10 &= \underline{44^\circ} \\
 m\angle 11 &= \underline{44^\circ} \\
 m\angle 13 &= \underline{34^\circ} \\
 m\angle 14 &= \underline{146^\circ} \\
 m\angle 15 &= \underline{146^\circ} \\
 m\angle 16 &= \underline{34^\circ}
 \end{aligned}$$



Find the value of the variable(s)

$$x = \frac{28}{1}$$

$$y = \frac{47}{1}$$



$$5x + 40 = 180$$
$$5x = 140$$

$$\begin{array}{r} 5x = 140 \\ \underline{-40} \quad \underline{-40} \\ 5x = 140 \\ \underline{5} \quad \underline{5} \\ x = 28 \end{array}$$

$$3y - 1 = 140$$
$$+1 \quad +1$$

$$\begin{array}{r} 3y - 1 = 140 \\ \underline{+1} \quad \underline{+1} \\ 3y = 141 \\ \underline{3} \quad \underline{3} \\ y = 47 \end{array}$$

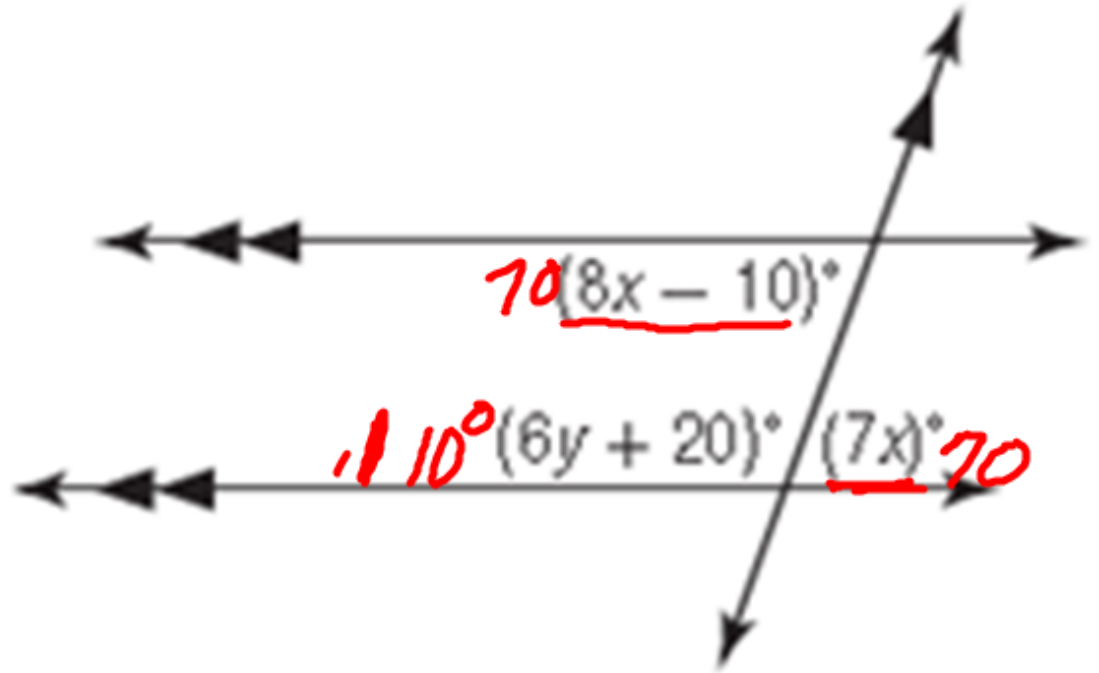
$$x = \underline{10}$$

$$y = \underline{15}$$

$$8x - 10 = 7x$$

$$\begin{array}{r} -8x \qquad -8x \\ \hline -10 = -1x \\ -1 \qquad -1 \end{array}$$

$$10 = x$$

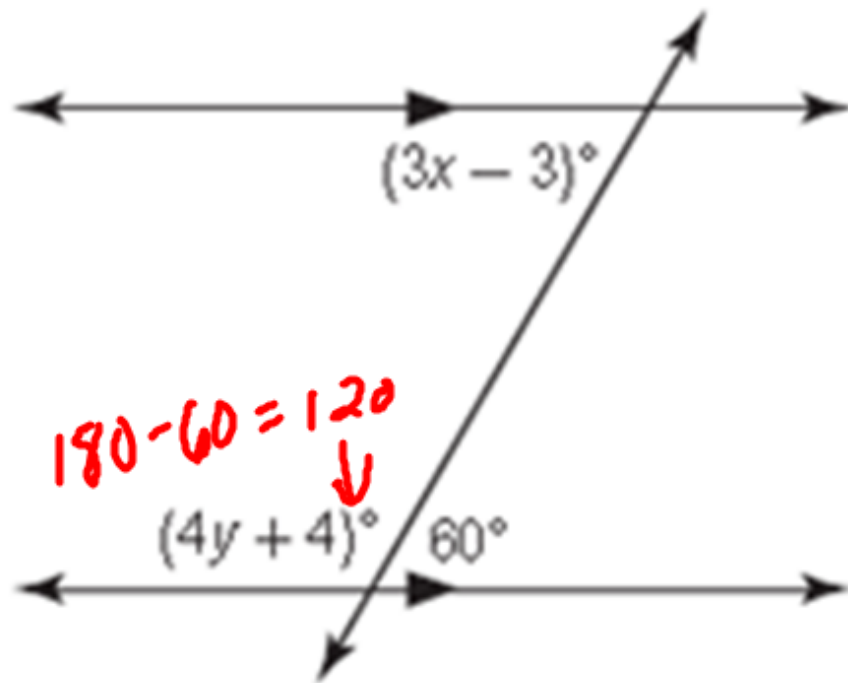


$$\begin{array}{r} 110 = 6y + 20 \\ -20 \qquad -20 \\ \hline 90 = 6y \end{array}$$

$$\begin{array}{r} 90 = 6y \\ 6 \qquad 6 \\ \hline 15 = y \end{array}$$

$$x = \underline{21}$$

$$y = \underline{29}$$



$$\begin{array}{r} 3x - 3 = 60 \\ +3 \quad +3 \\ \hline 3x = 63 \\ \frac{3x}{3} = \frac{63}{3} \\ x = 21 \end{array}$$

$$\begin{array}{r} 4y + 4 = 120 \\ -4 \quad -4 \\ \hline 4y = 116 \\ \frac{4y}{4} = \frac{116}{4} \\ y = 29 \end{array}$$

Proving Lines Parallel

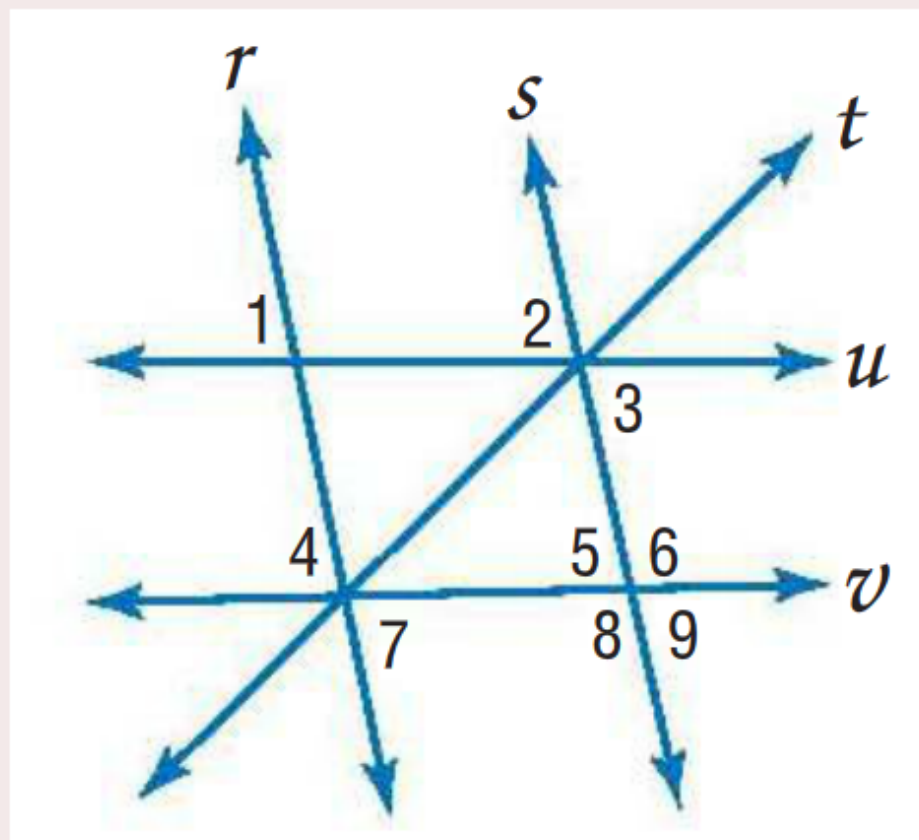
Given the following information, determine which lines, if any are parallel.

$$\angle 1 \cong \angle 2$$

yes $r \parallel s$

$$\angle 5 \cong \angle 7$$

yes $r \parallel s$



$$m\angle 3 + m\angle 6 = 180$$

$u // v$

$$\angle 3 \cong \angle 7$$

Can't prove
lines //

