

Distance and Midpoints



Students will identify and model distance, midpoint, and segment bisector.

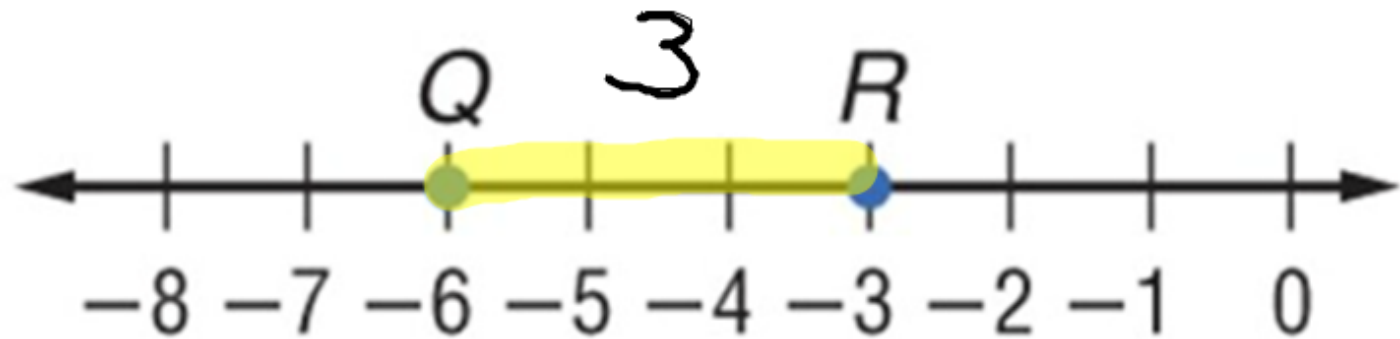
Students will find the midpoint on a line segment and the distance between two points.

Distance.....

length of the segment connecting the two points

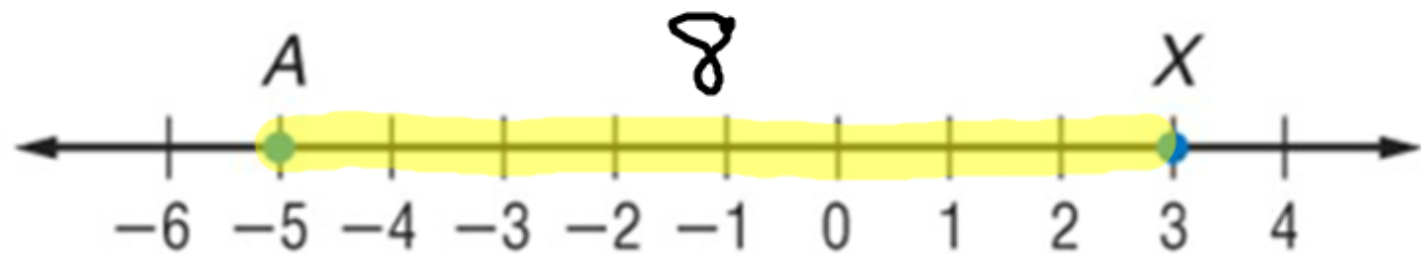
can never be negative

Use the number line to find QR.



$$|-6 - (-3)| \qquad -3 - (-6)$$
$$|-3| = 3 \qquad 3$$

Use the number line to find AX

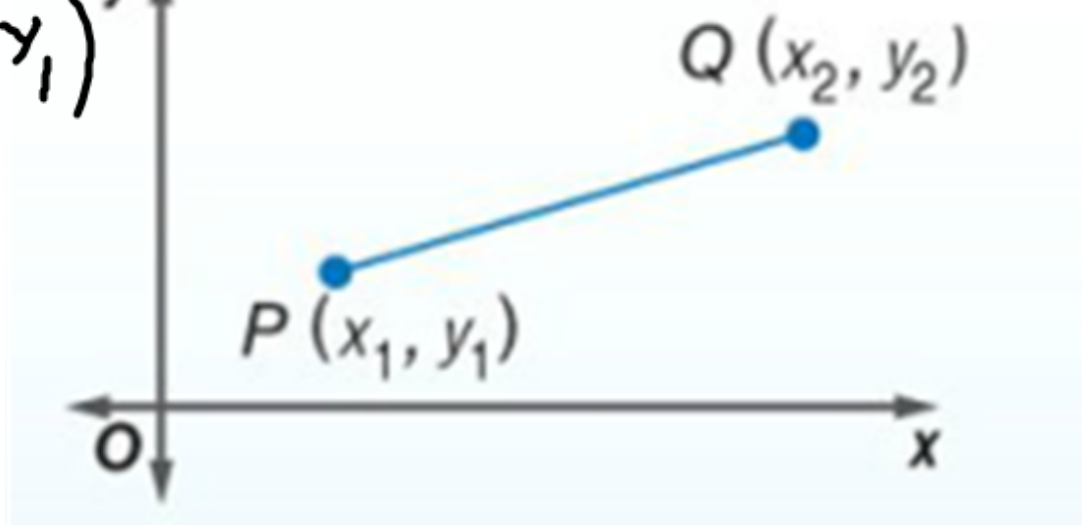


$$|-5 - 3| \qquad |3 - (-5)|$$
$$|-8| \qquad |8|$$
$$8 \qquad 8$$

Key Concept

Distance Formula (in Coordinate Plane)

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



Find the distance between $E(-4, 1)$ and $F(3, -1)$.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

x_1 y_1 x_2 y_2

$$d = \sqrt{(3 - (-4))^2 + (-1 - 1)^2}$$

$$d = \sqrt{(7)^2 + (-2)^2}$$

$$d = \sqrt{49 + 4}$$

$$d = \sqrt{53} \approx 7.3$$

d

Find the distance between $A(-3, 4)$ and $M(1, 2)$.

x_2 y_2

x_1 y_1

$$d = \sqrt{(-3-1)^2 + (4-2)^2}$$

$$d = \sqrt{(-4)^2 + (2)^2}$$

$$d = \sqrt{16 + 4}$$

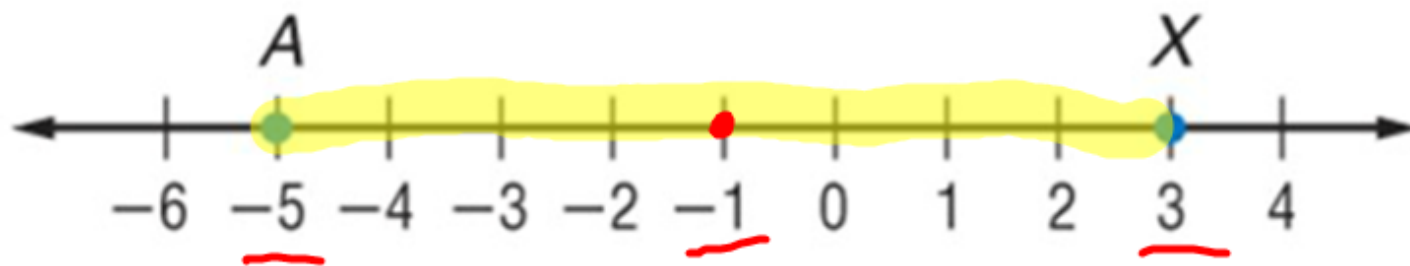
$$d = \sqrt{20} \approx 4.5$$

Key Concept

Midpoint Formula (on Number Line)

Midpoint - halfway btwn 2 pts

Find the midpoint of AX



$$\frac{-5 + 3}{2} = \frac{-2}{2} = -1$$

Find the coordinates of M , the midpoint of \overline{GH} ,
for $G(\overset{x_1}{8}, \overset{y_1}{-6})$, and $H(\overset{x_2}{-14}, \overset{y_2}{12})$.

$$\left(\frac{8 + (-14)}{2}, \frac{-6 + 12}{2} \right)$$

$$\left(\frac{-6}{2}, \frac{6}{2} \right)$$

$$(-3, 3)$$

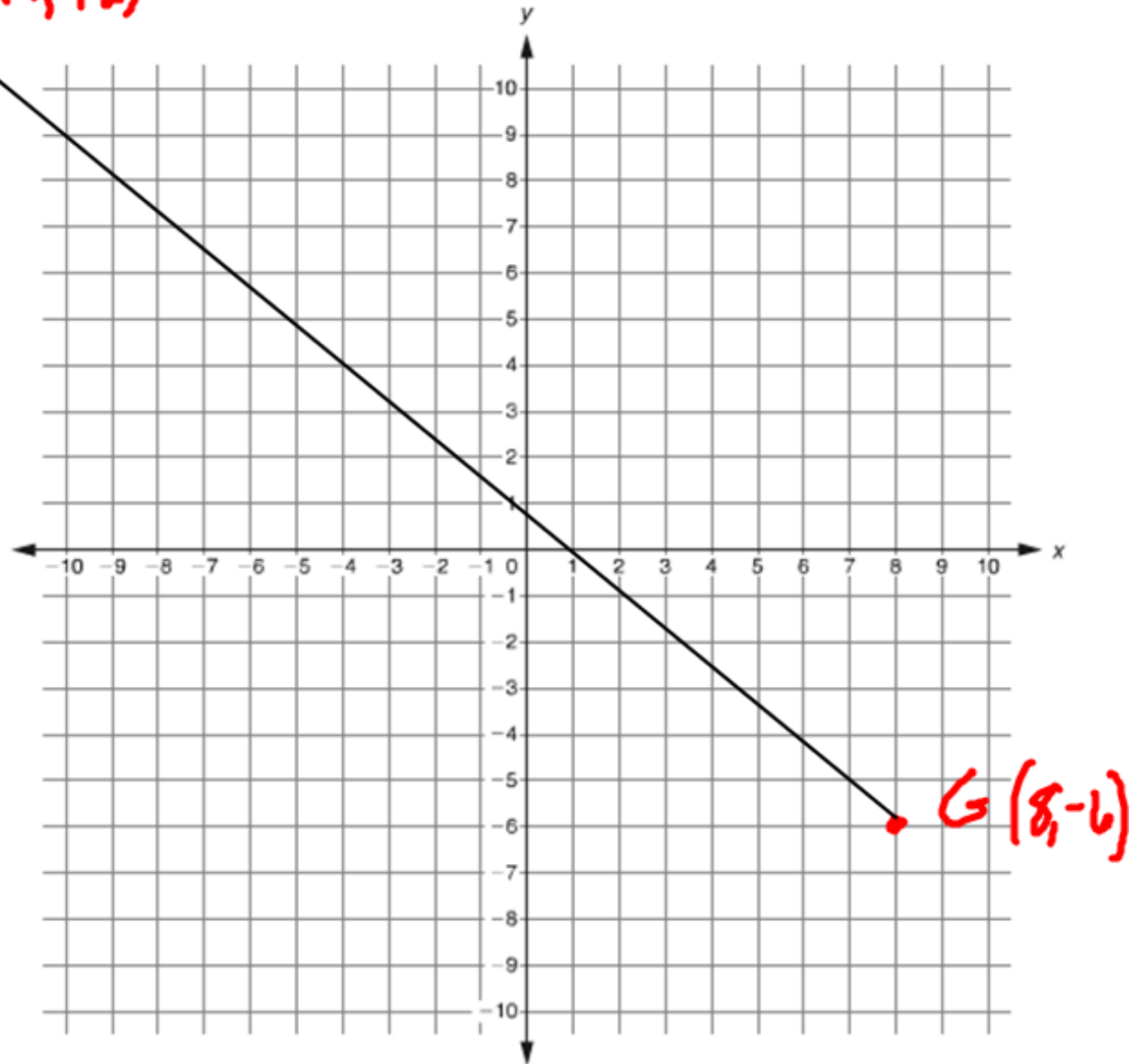
Key Concept

Midpoint Formula (in Coordinate Plane)

Midpoint Formula

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

H(-14, 12)



Find the coordinates of the midpoint of \overline{XY}
for $X(-2, 3)$, and $Y(-8, -9)$.

$$\left(\frac{-2 + -8}{2}, \frac{3 + -9}{2} \right)$$

$$\left(\frac{-10}{2}, \frac{-6}{2} \right)$$

$$(-5, -3)$$

